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# Understanding the Effect of Bias in Deep Anomaly Detection

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Ziyu Ye, Yuxin Chen, Haitao Zheng

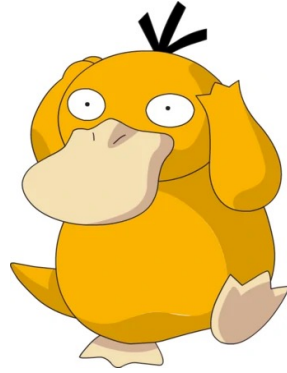


THE UNIVERSITY OF  
CHICAGO

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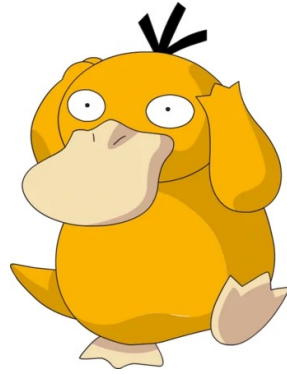


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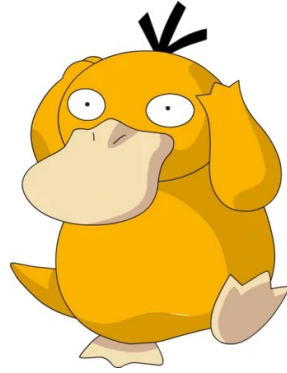
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(An illustrative example of Pokémon.)

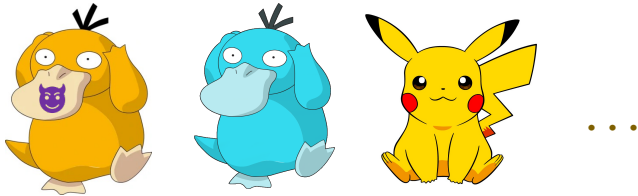
Normal



Abnormal



Known types in source distribution



Unknown types in target distribution

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→ Challenging to get a *representative anomaly set*.



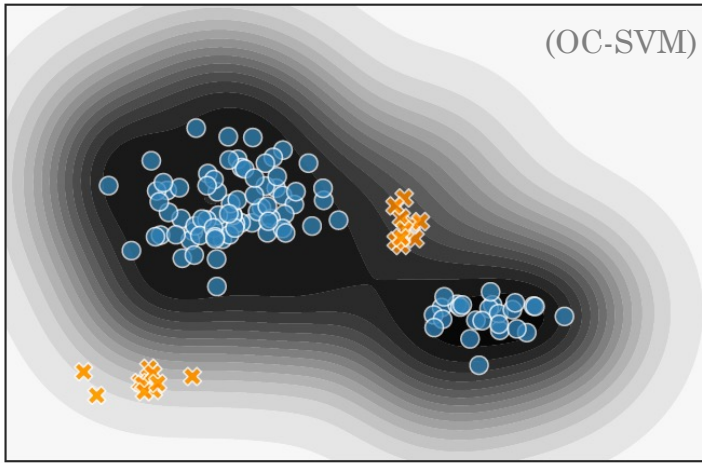
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## Semi-Supervised (AD)

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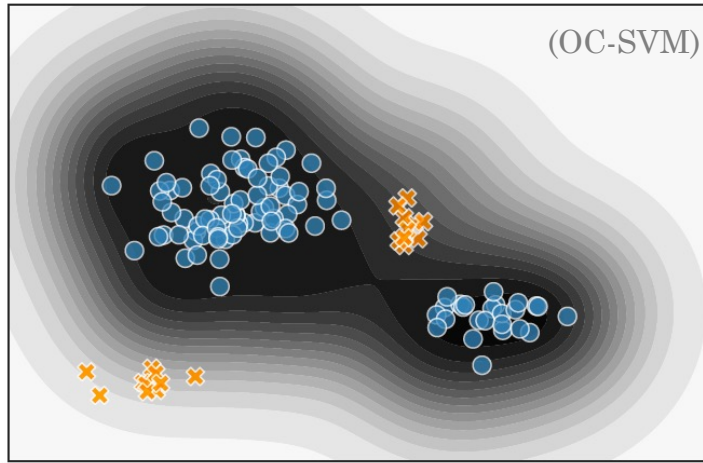
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Low  High  
Anomaly Score

● Normal Data  
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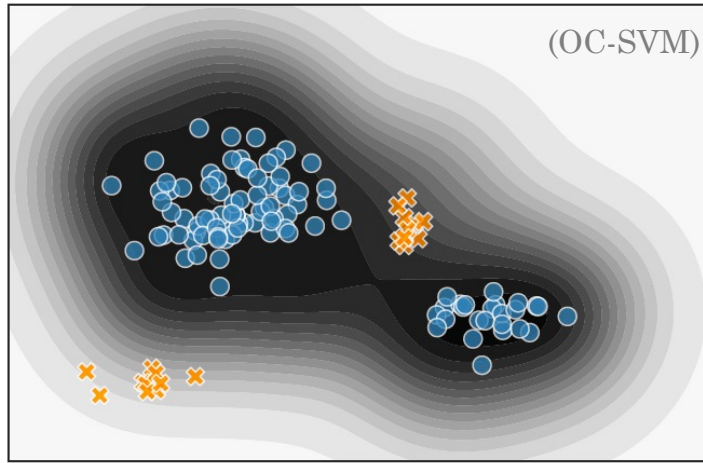
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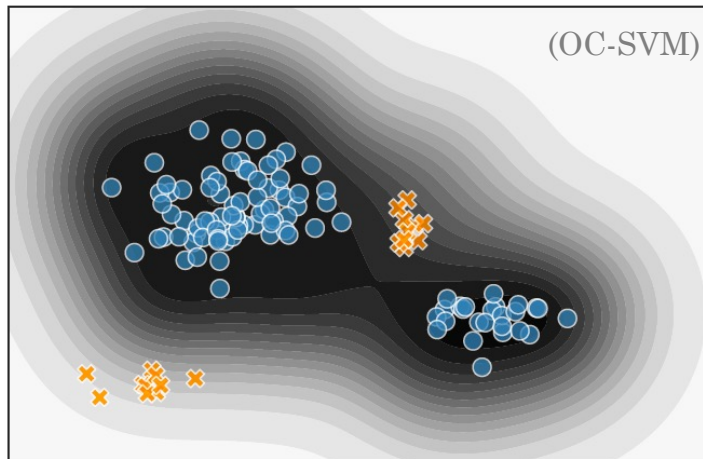
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Can we make use of *additional labeled anomalies*?

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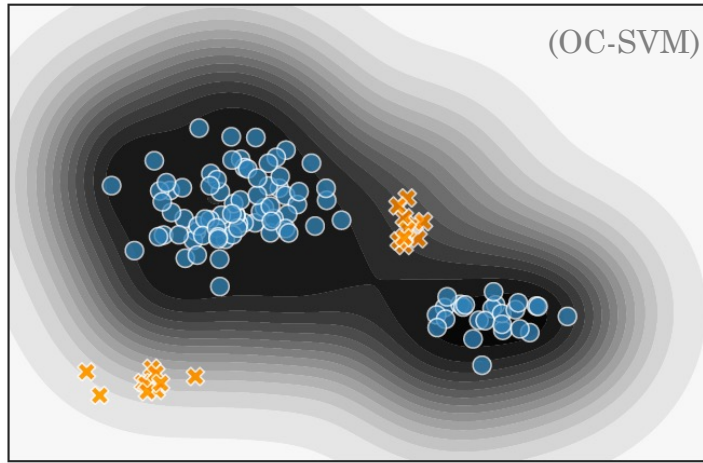
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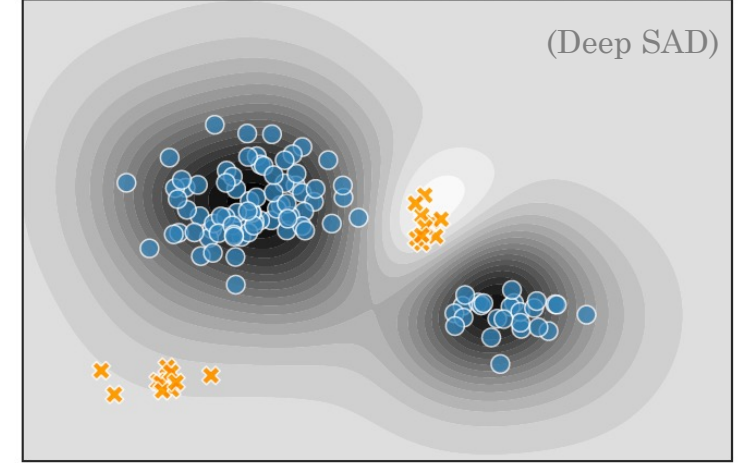
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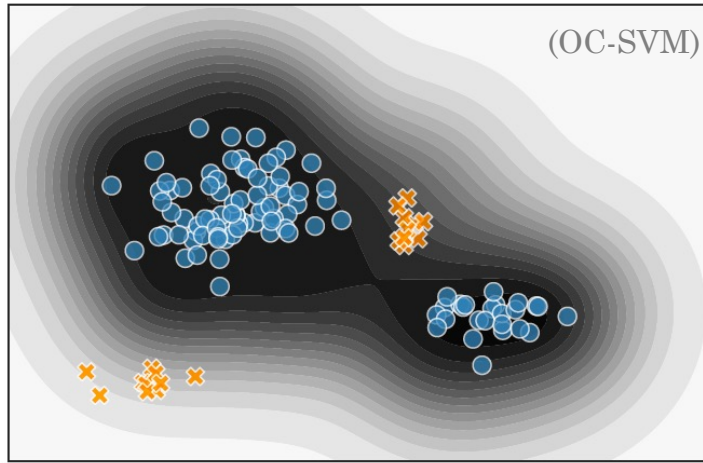
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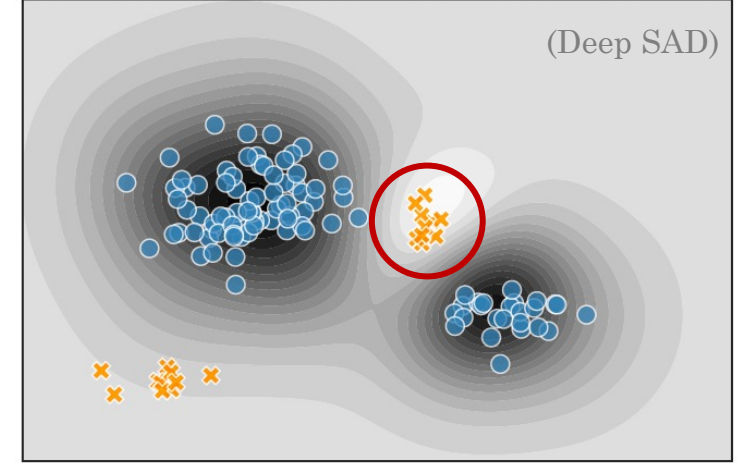
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# Motivation

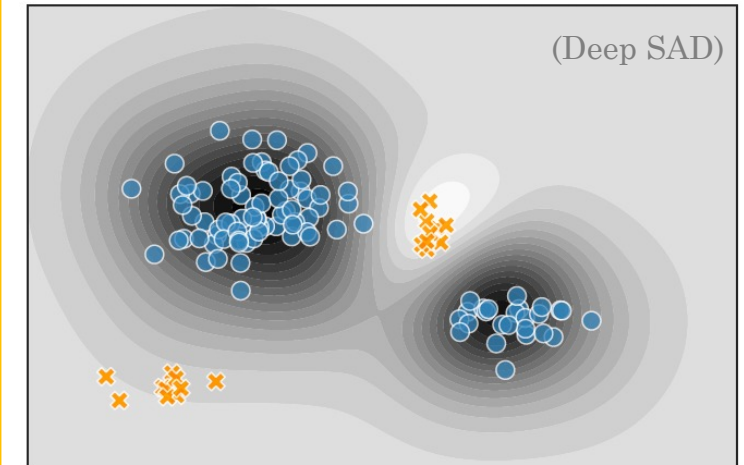
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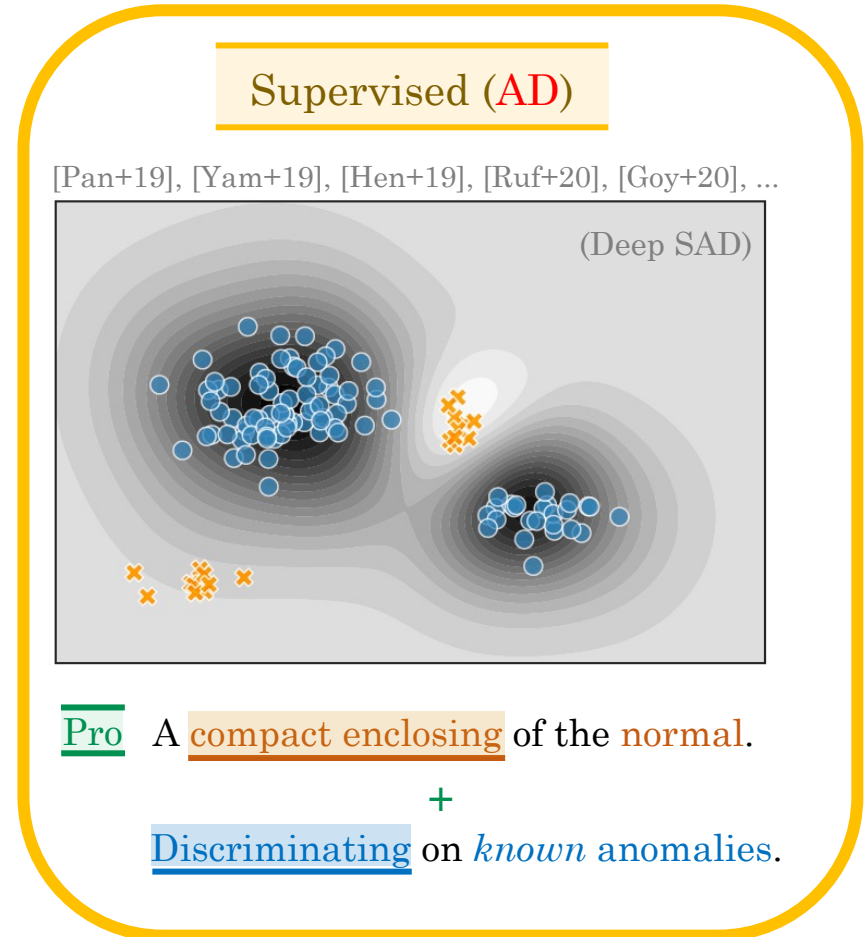
# Motivation

Low  High  
Anomaly Score

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## Will *additional labels* do *harm*?

Can **unseen anomalies** suffer from **bias\***?



\* Note that such bias is novel compared to the aforementioned in literature (c.f. Section 2 of our paper).

Image Source: Ruff, Lukas, et al. "Deep semi-supervised anomaly detection." In *proc. of ICLR*, 2020.

# A Counter-Intuitive Example

Training with *additional labeled anomalies* can bring *disastrous harmful bias*.

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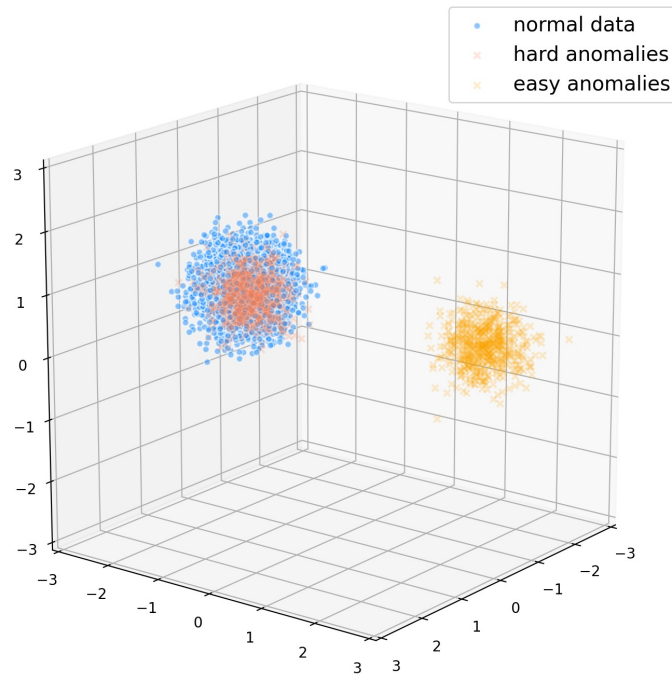


Fig 1. Original 3D Space

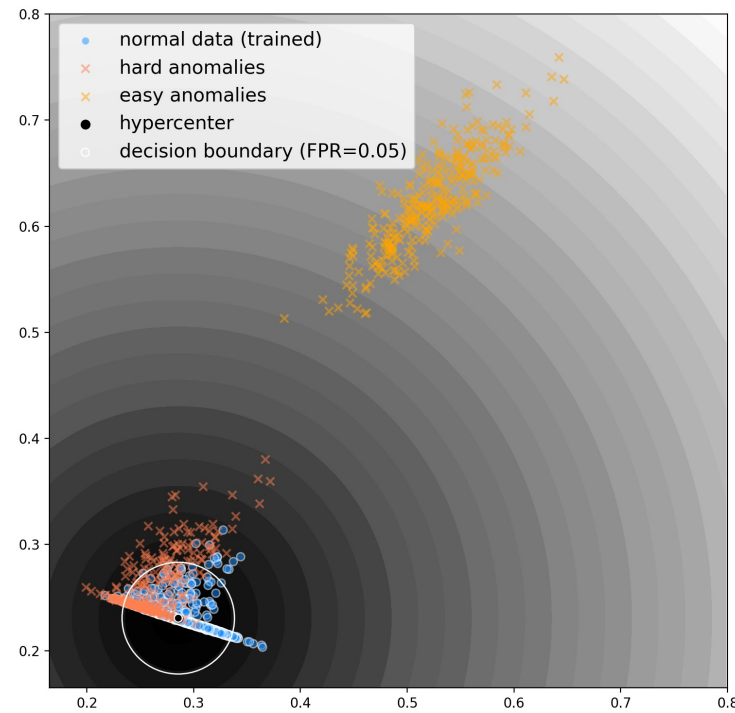


Fig 2. 2D Latent Space (*Semi-Supervised AD*)

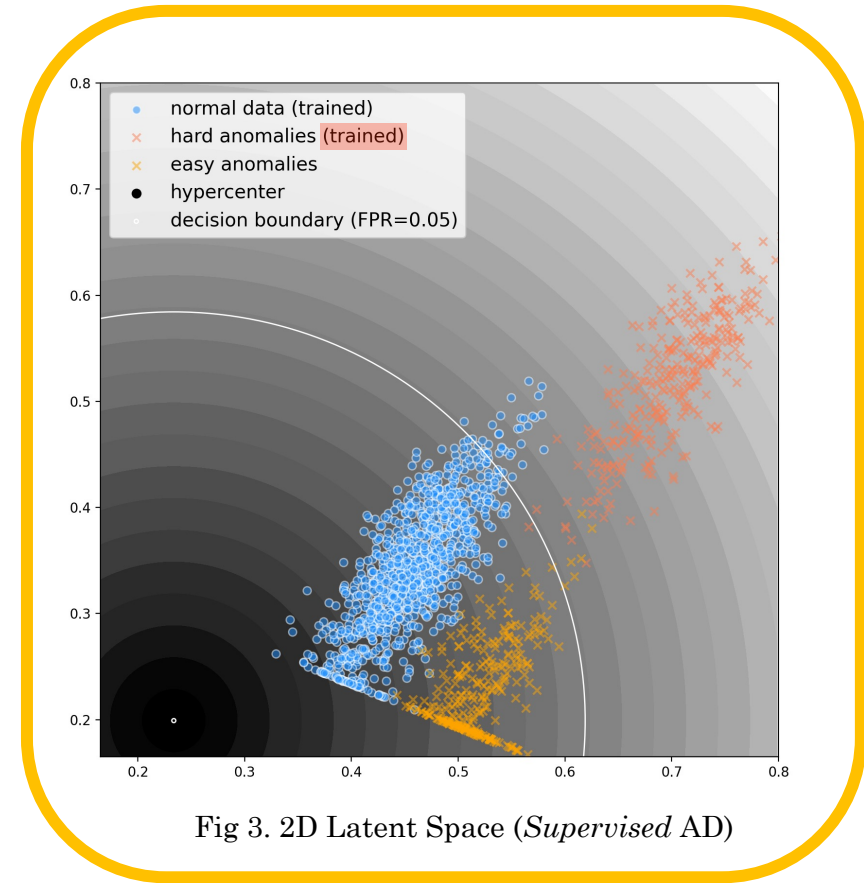


Fig 3. 2D Latent Space (*Supervised AD*)

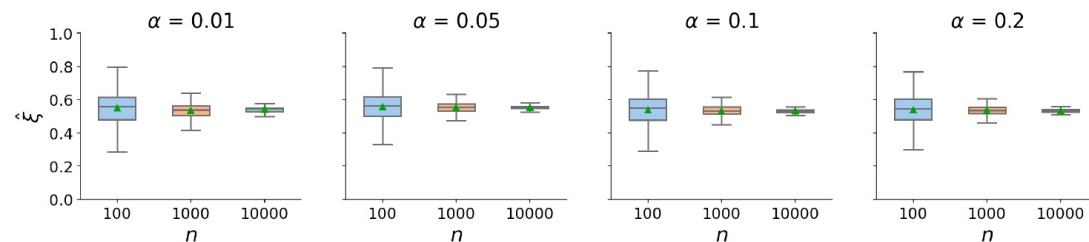
# Our Contributions

## 1 Define Bias: A formal ERM Framework

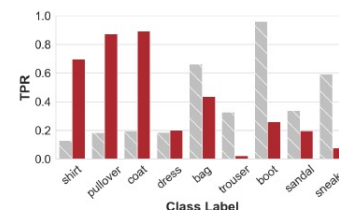
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## 2 Estimate Bias: The First PAC Analysis

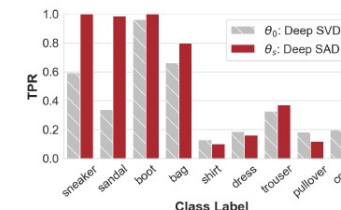
$$n \geq \frac{8}{\epsilon^2} \cdot \left( \log \frac{2}{1-\sqrt{1-\delta}} \cdot \left( \frac{2-\alpha}{\alpha} \right)^2 + \log \frac{2}{\delta} \cdot \frac{1}{1-\alpha} \left( \left( \frac{\ell_a}{\ell'_0} \right)^2 + \left( \frac{\ell'_a}{\ell'_0} \right)^2 \right) \right)$$



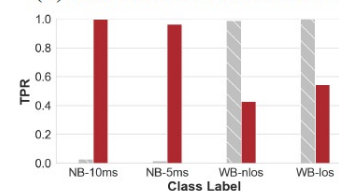
## 3 Characterize Bias: Empirical Experiments



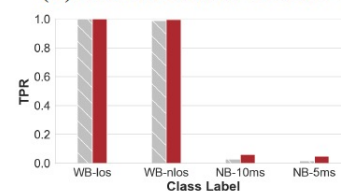
(a) Fashion-MNIST: Scenario 1



(b) Fashion-MNIST: Scenario 2



(c) Spectrum Misuse: Scenario 1



(d) Spectrum Misuse: Scenario 2

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Problem formulation is different.

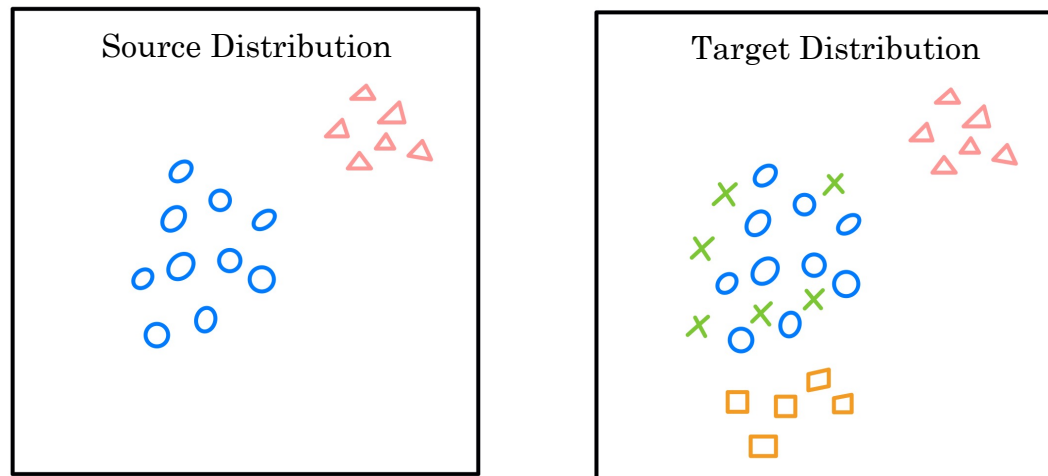


Fig 1. Data distribution of AD problem. The blue represent the normal data, and other different colors represent different *subtypes* of anomalies.

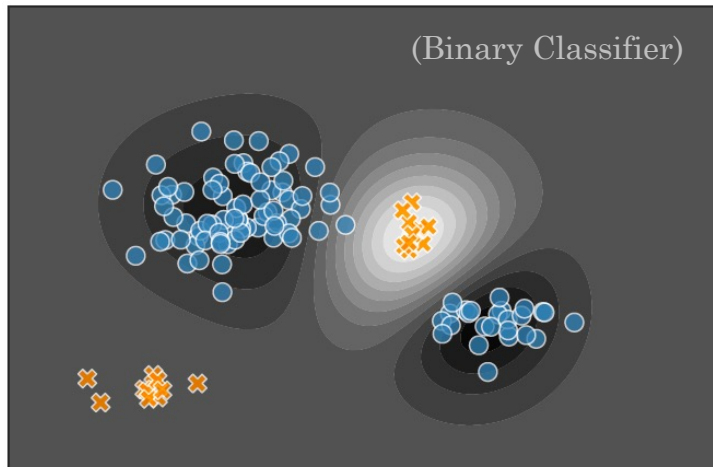
Task Type	Distribution Shift	Known Target Distribution	Known Target Label Set
<b>Imbalanced Classification</b> [Johnson and Khoshgoftaar, 2019]	No	N/A	N/A
<b>Closed Set Domain Adaptation</b> [Saenko <i>et al.</i> , 2010]	Yes	Yes	Yes
<b>Open Set Domain Adaptation</b> [Panareda Busto and Gall, 2017]	Yes	Yes	No
<b>Anomaly Detection</b> [Chalapathy and Chawla, 2019]	Yes	No	No

Table 1: Comparison of anomaly detection tasks with other relevant classification tasks.

# [Clarification] Bias in *AD* $\neq$ Bias in *Supervised Learning*

Training mechanism is different.

Supervised (Classifier)

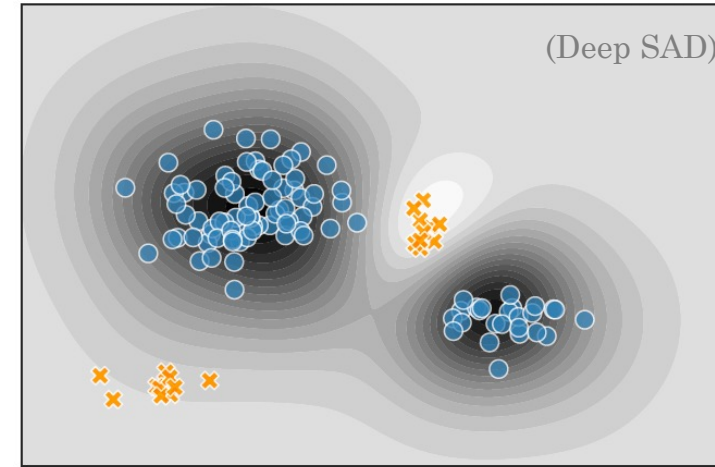


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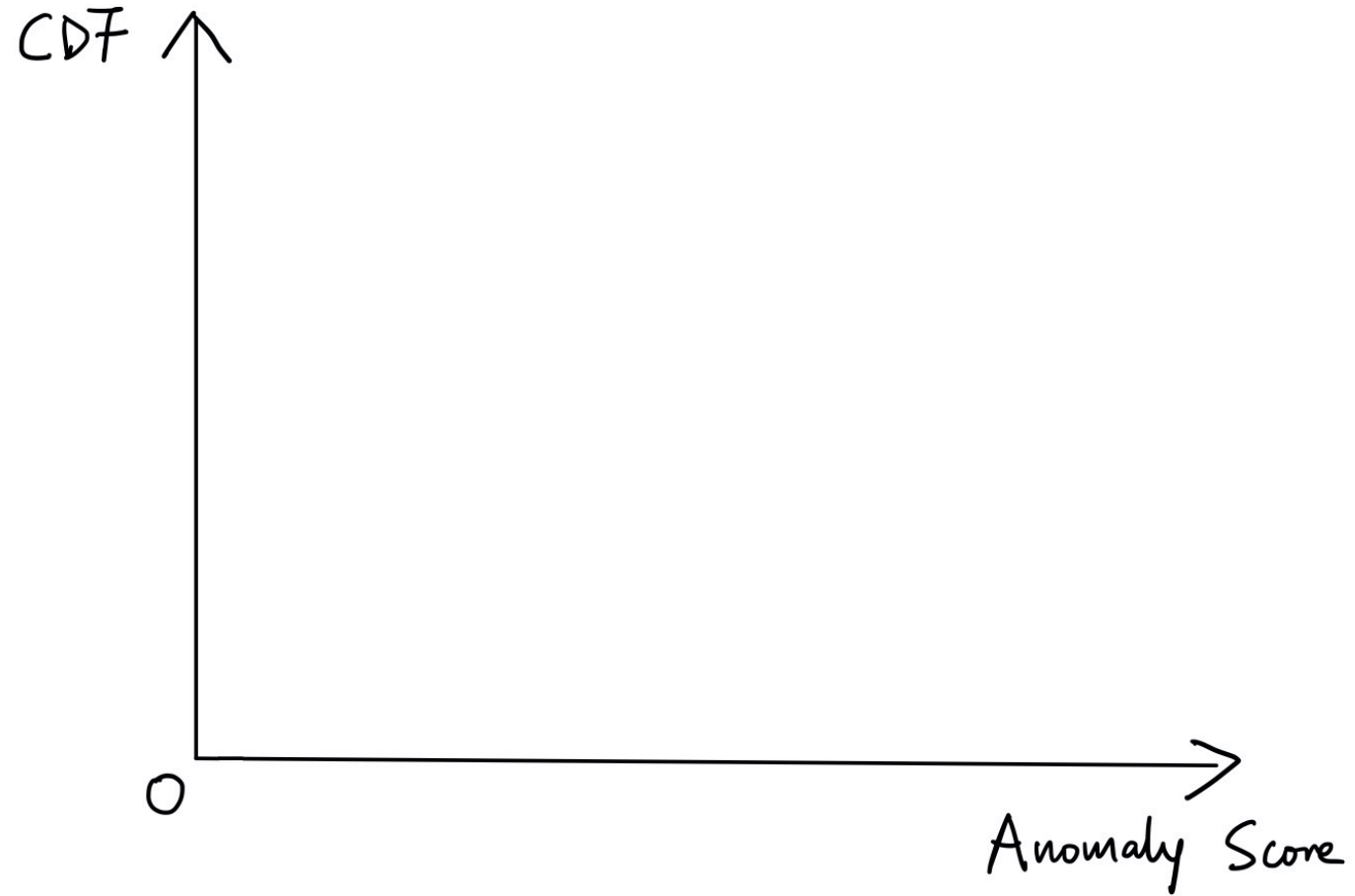


# How to *Define* Bias in AD?

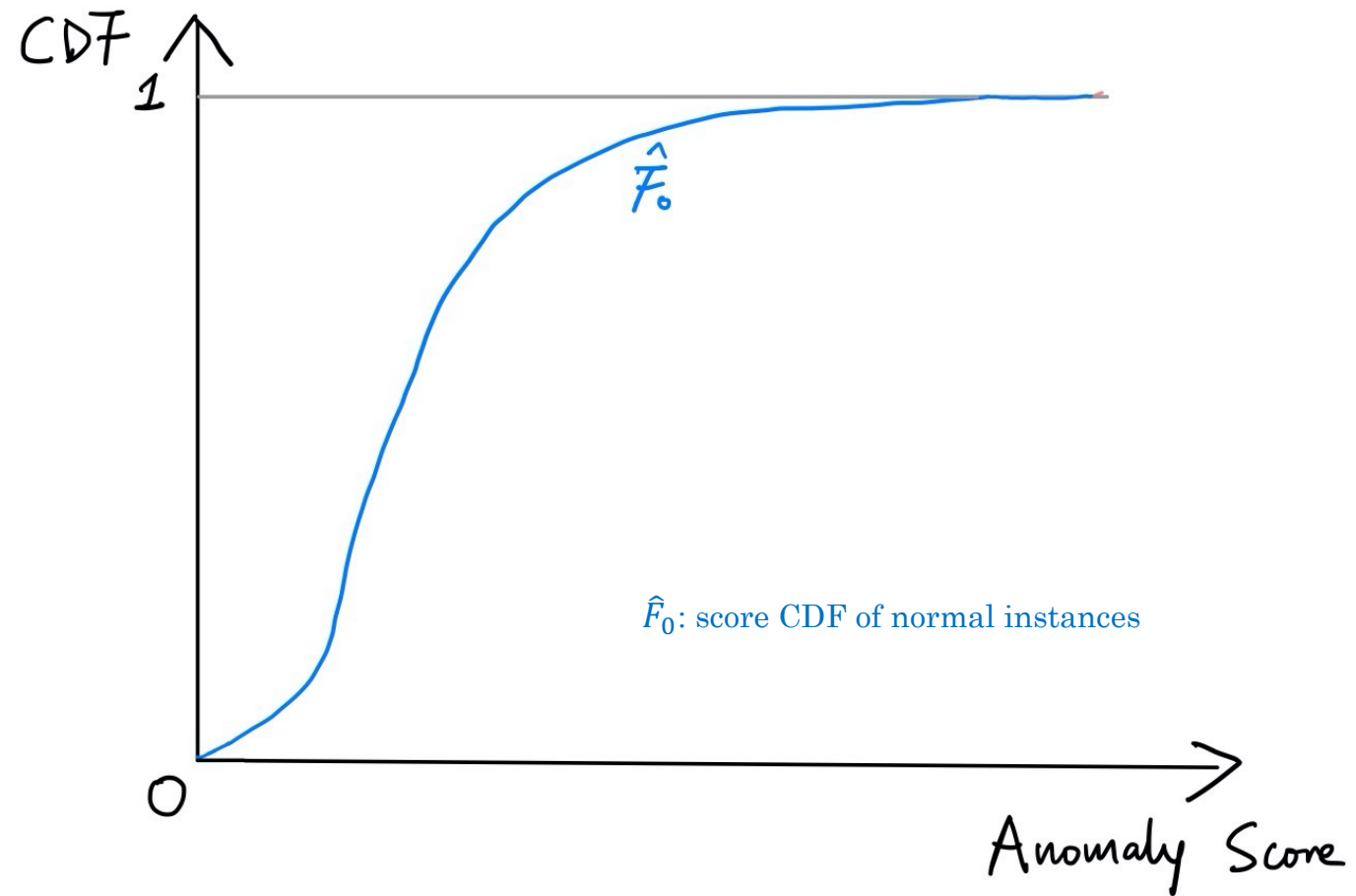
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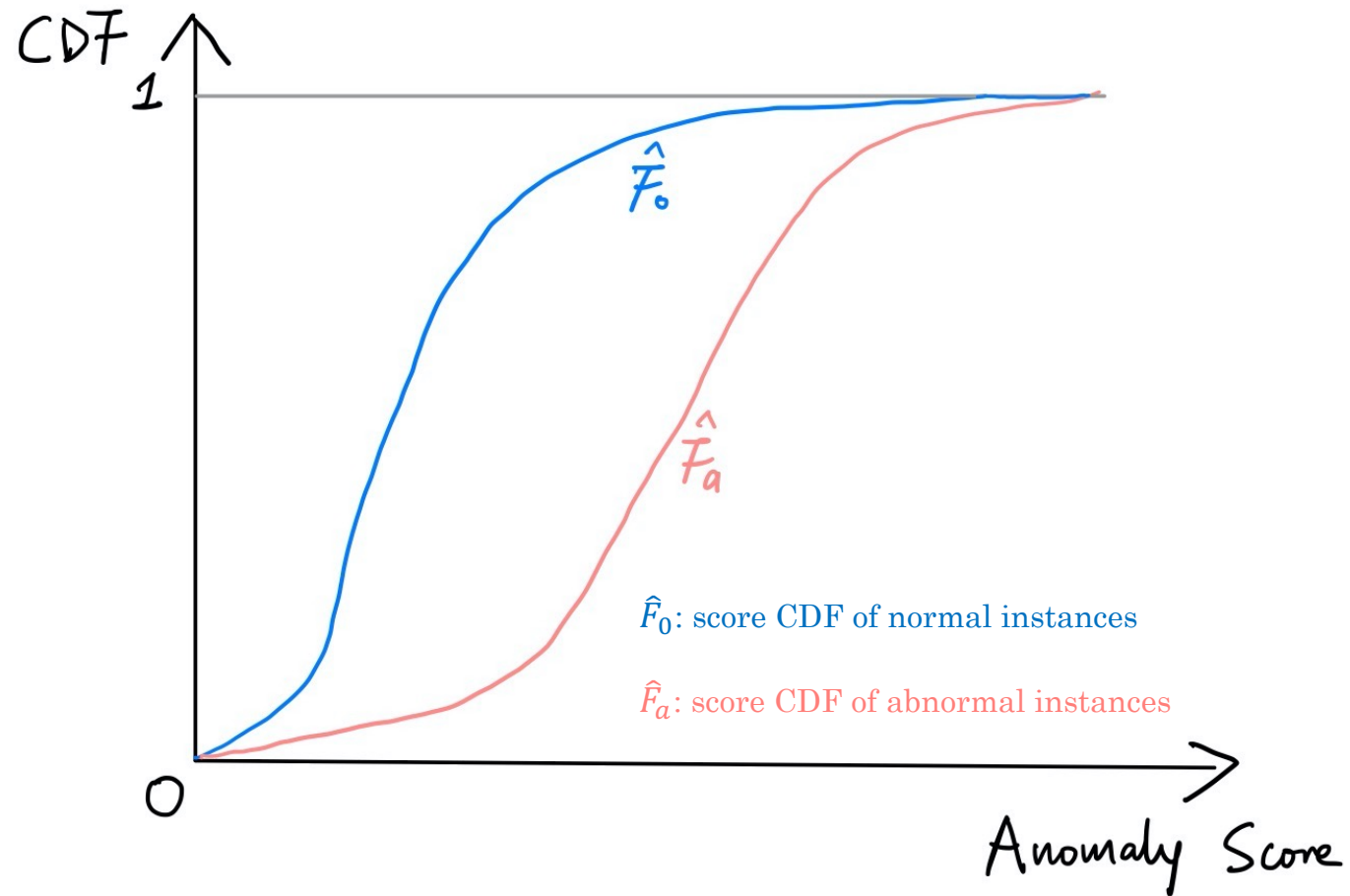
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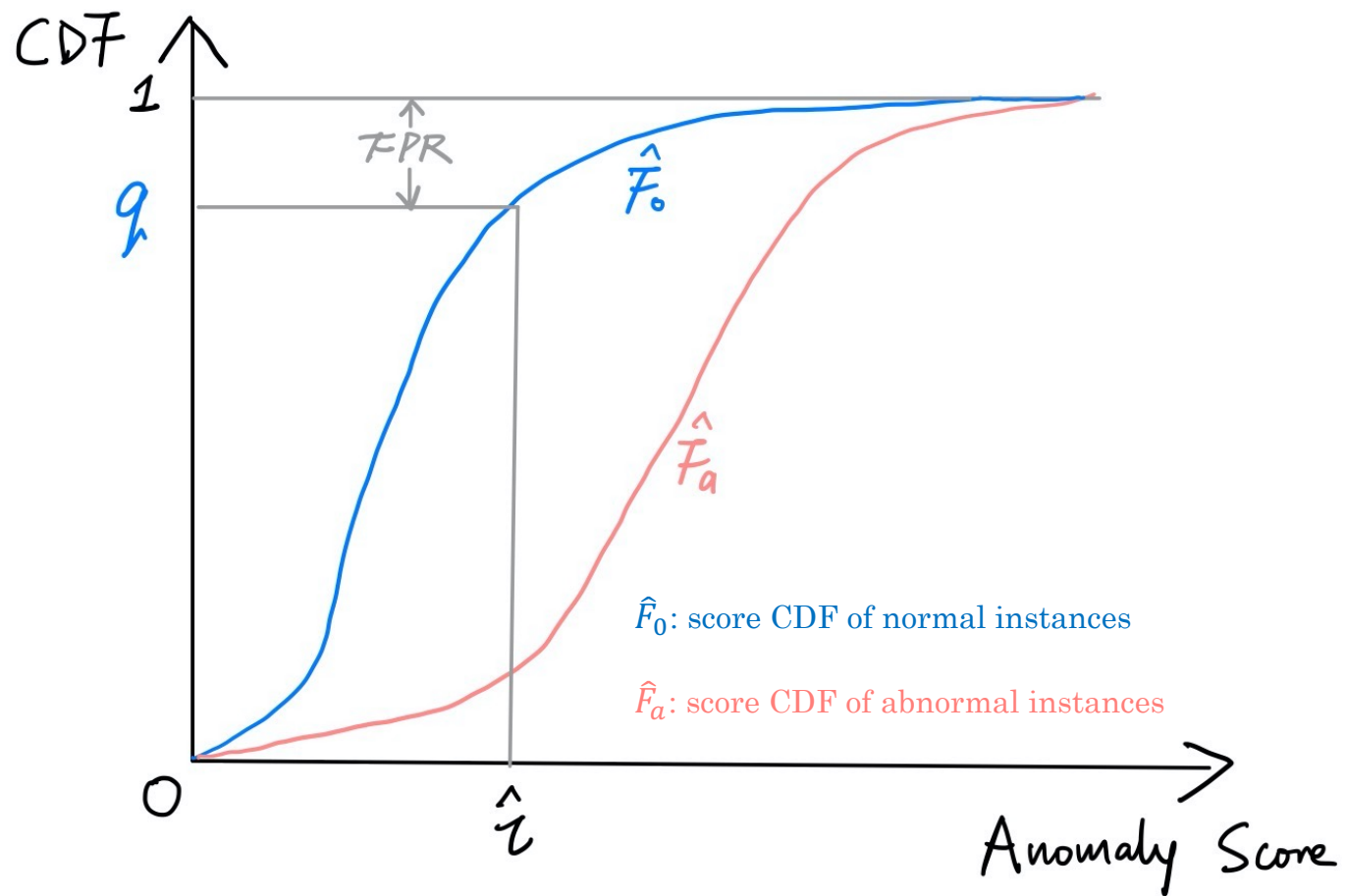
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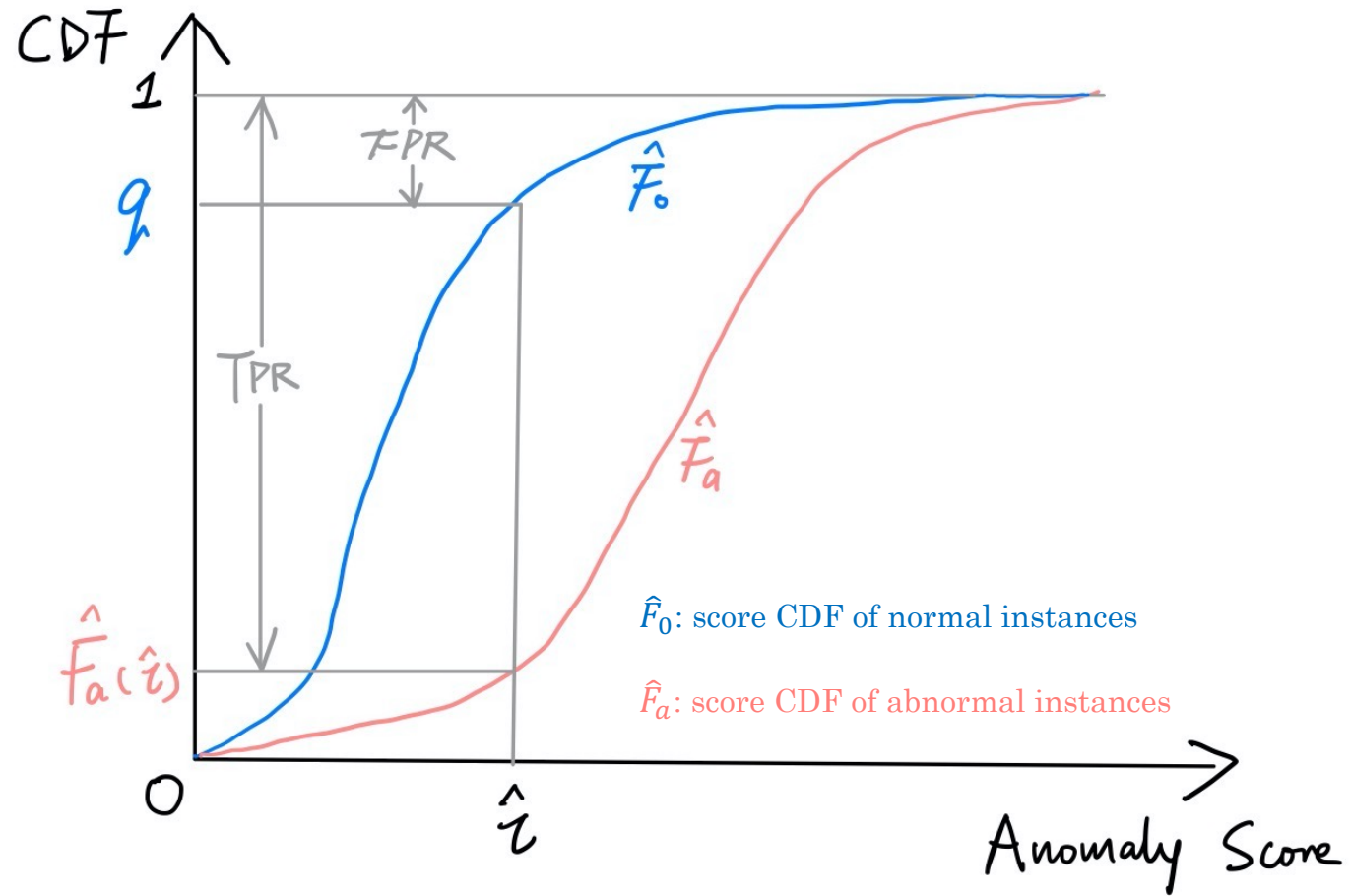
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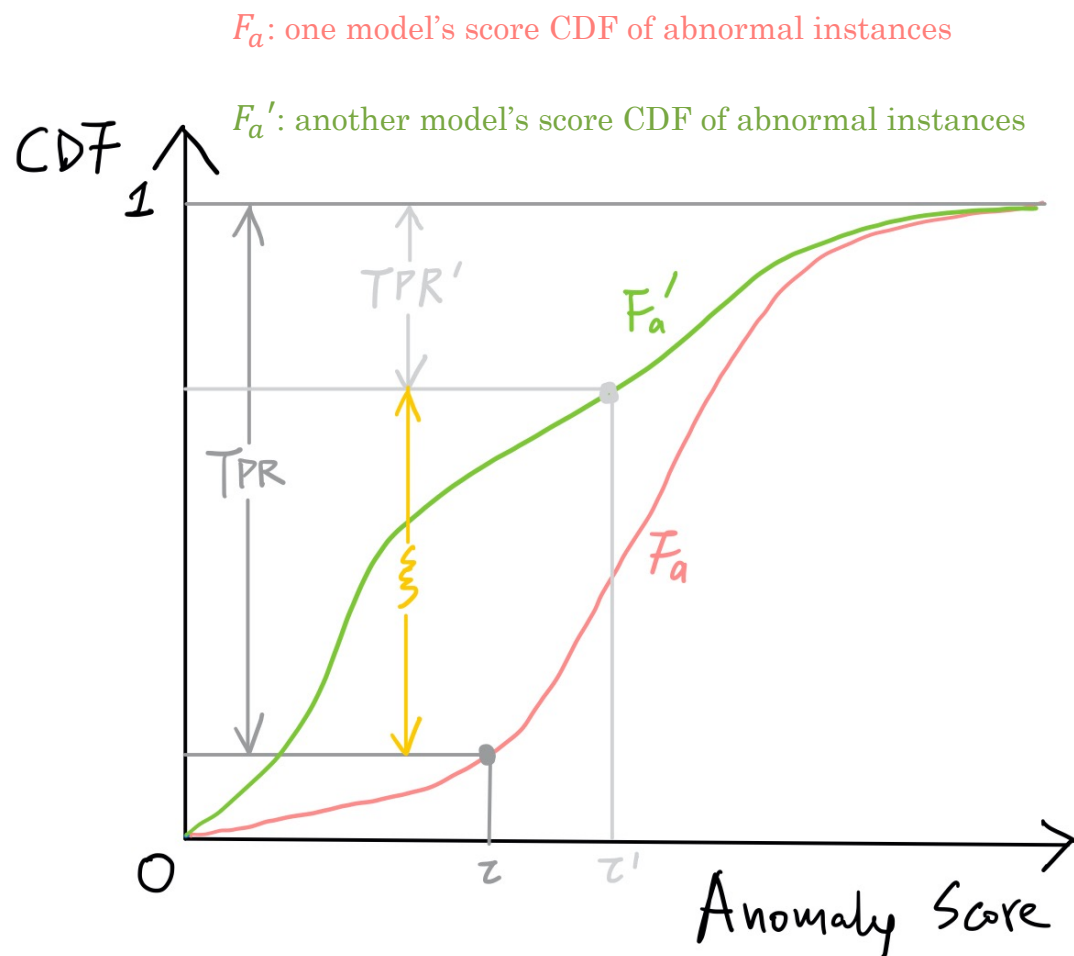


# ERM-Style Scoring Bias

## 1 Scoring Bias

$$\text{bias}(\hat{s}_\theta, \hat{\tau}_\theta) := \arg \max_{(s_\theta, \tau_\theta): \theta \in \Theta} \text{TPR}(s_\theta, \tau_\theta) - \text{TPR}(\hat{s}_\theta, \hat{\tau}_\theta)$$

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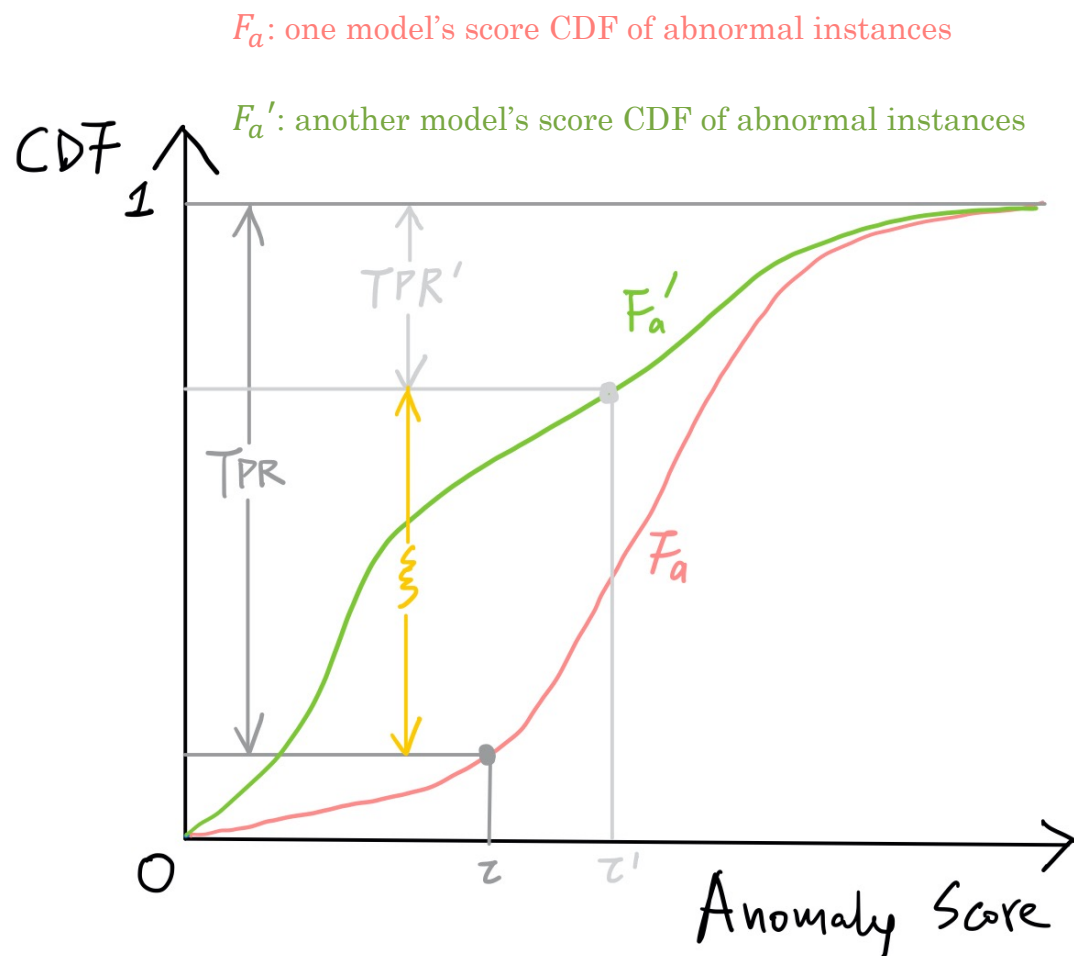
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$$\begin{aligned} \xi(s, s') &:= \text{bias}(s, \tau) - \text{bias}(s', \tau') \\ &= \text{TPR}(s', \tau') - \text{TPR}(s, \tau) \end{aligned}$$

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## 3 Empirical Relative Scoring Bias

$$\hat{\xi}(s, s') := \widehat{\text{TPR}}(s', \tau') - \widehat{\text{TPR}}(s, \tau)$$





# How to *Estimate* Bias in AD?

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# Finite Sample Guarantee

● **Goal:** a **theoretical guarantee** on **model performance** in terms of **bias**.

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**Proposition 1.** *Given two scoring functions  $s, s'$  and a target FPR  $q$ , the relative scoring bias is*

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**Theorem 3.** Assume that  $F_a, F'_a, F_0^-, F_0'^-$  are Lipschitz continuous with Lipschitz constant  $l_a, l'_a, l_0^-, l_0'^-$ , respectively. Let  $\alpha$  be the fraction of abnormal data from the mixture distribution. Then, w.p. at least  $1 - \delta$ , with

$$n = \mathcal{O}\left(\frac{1}{\alpha^2 \epsilon^2} \log \frac{1}{\delta}\right)$$

the empirical relative scoring bias satisfies  $|\hat{\xi} - \xi| \leq \epsilon$ .

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# Convergence of Scoring Bias: *Empirical Results*

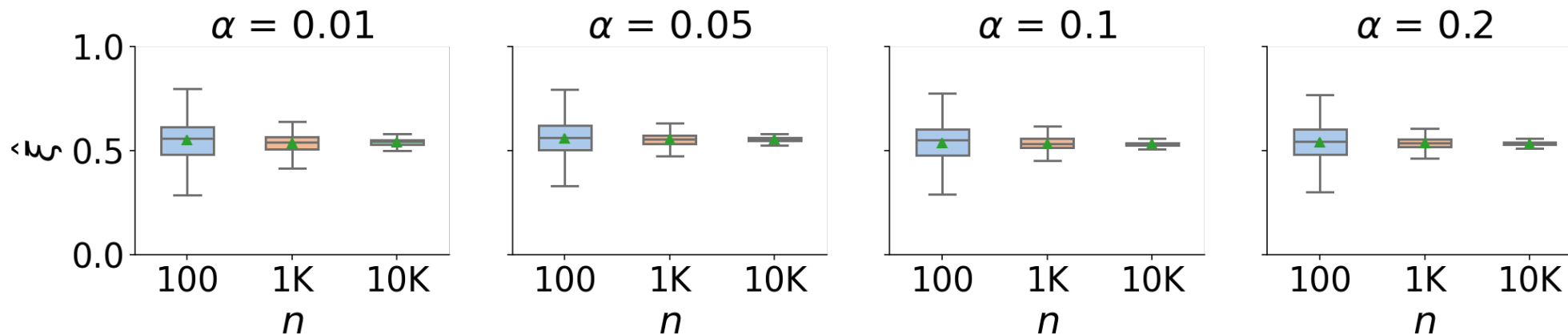


Fig 1.  $\xi$  is the scoring bias of Deep SVDD relative to Deep SAD.

- The estimation error  $\epsilon$  decreases at the rate of  $\frac{1}{\sqrt{n}}$ .
- The sample complexity  $n$  grows as  $\mathcal{O}\left(\frac{1}{\alpha^2 \epsilon^2} \log \frac{1}{\delta}\right)$ .



# How does Bias *Impact* AD?

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# Recall on Our Observations...

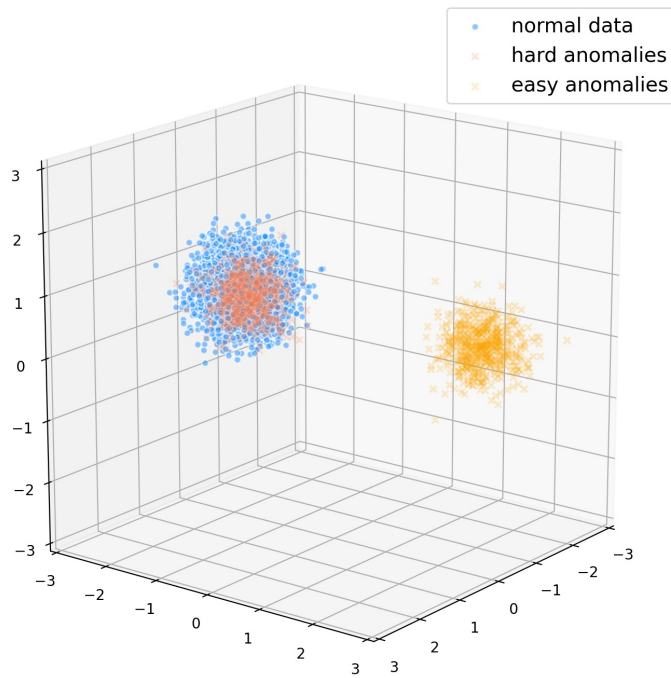


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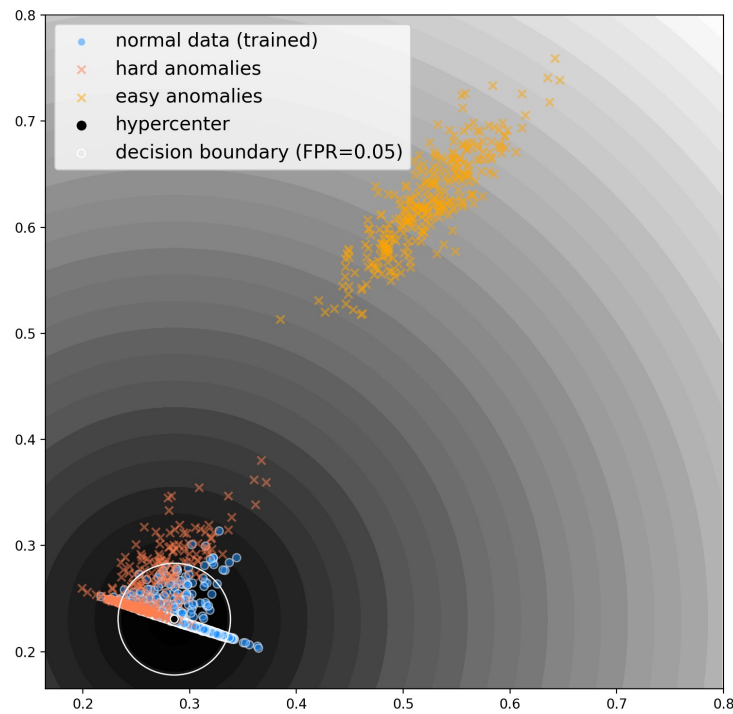


Fig 2. 2D Latent Space (*Semi-Supervised AD*)

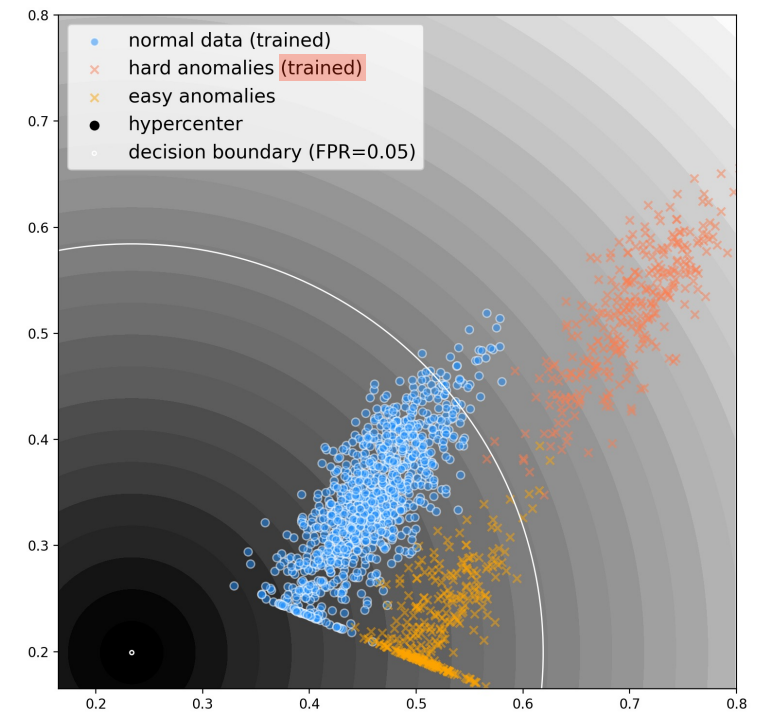


Fig 3. 2D Latent Space (*Supervised AD*)

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Training with **different distributions** affects **normal enclosing** *unevenly*.

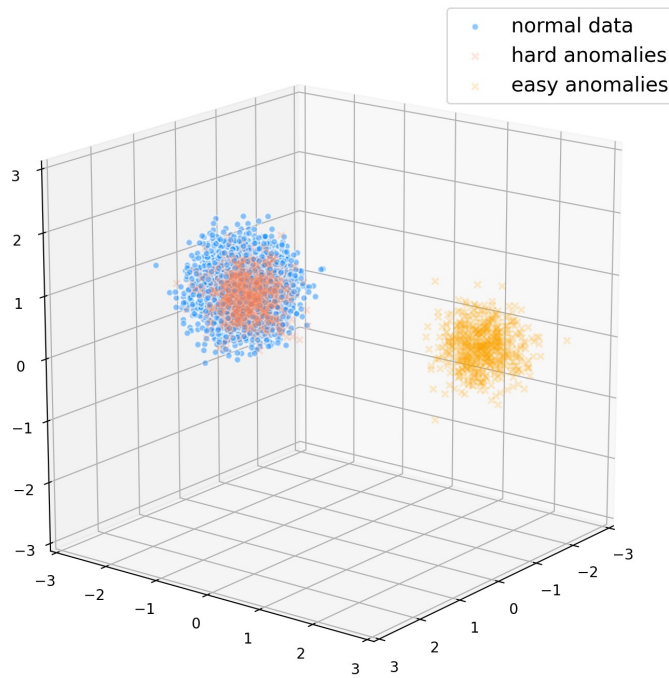


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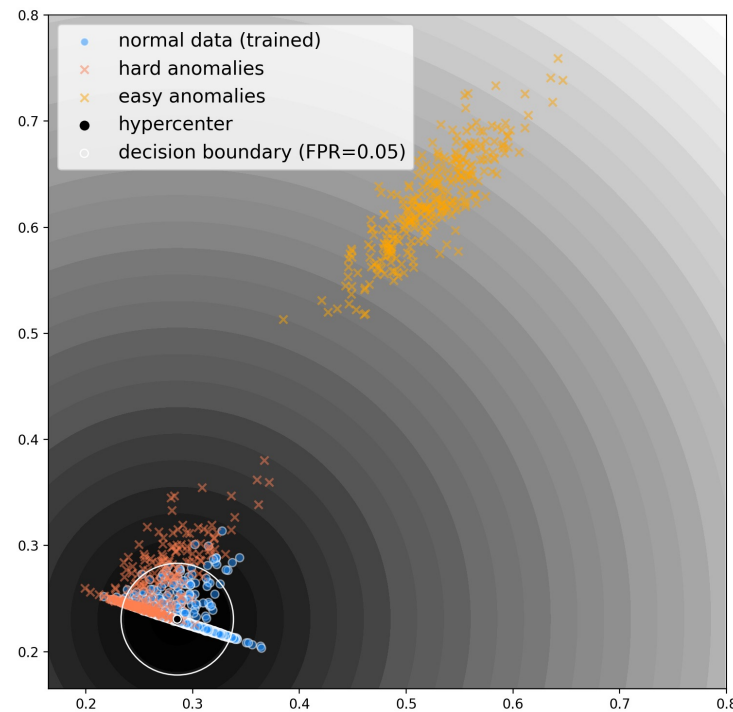


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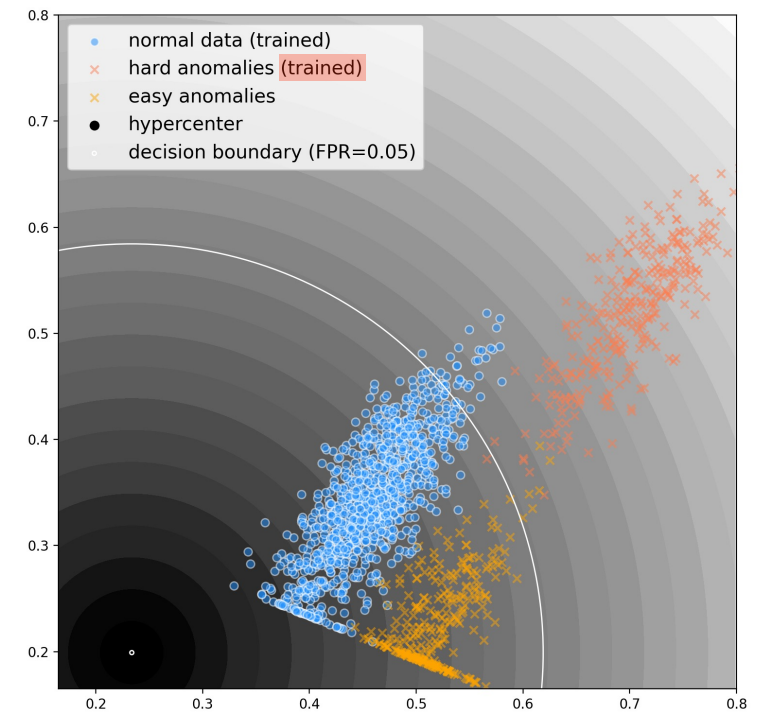


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# Our Hypothesis

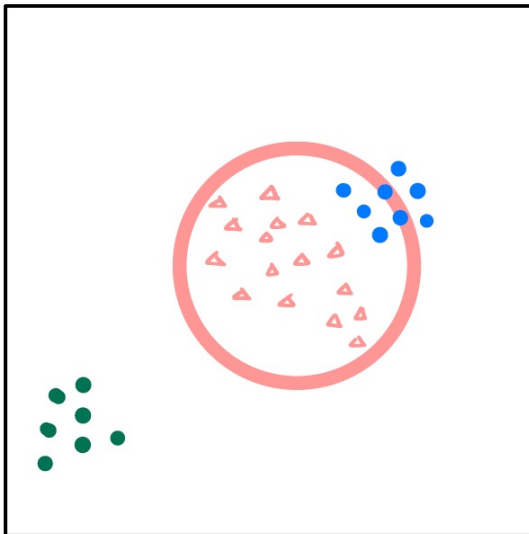
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$\triangle$  : normal data

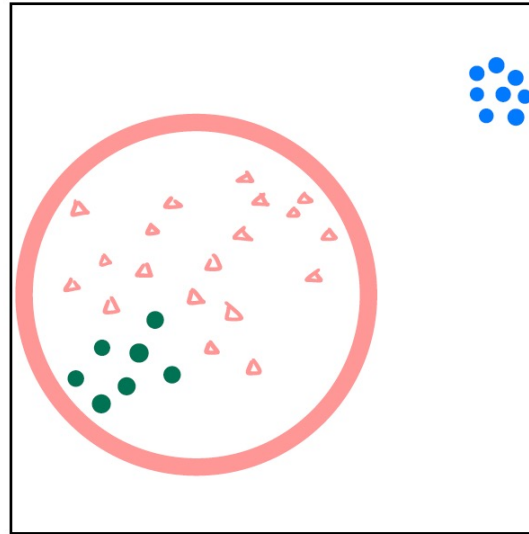
$\bullet$  : anomaly type 1 (hard)

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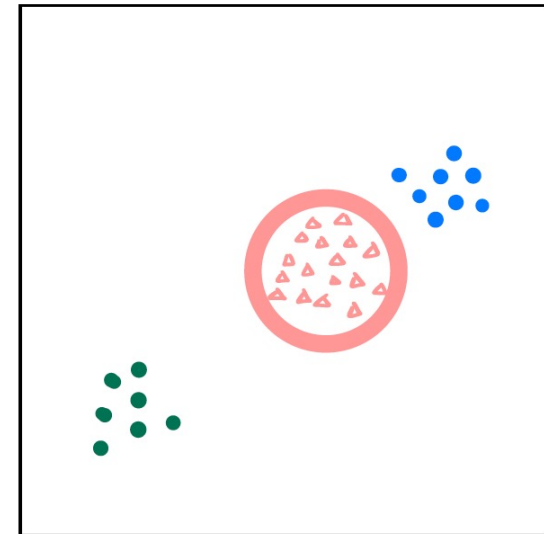
train with  $\triangle$



train with  $\triangle$  and  $\bullet$



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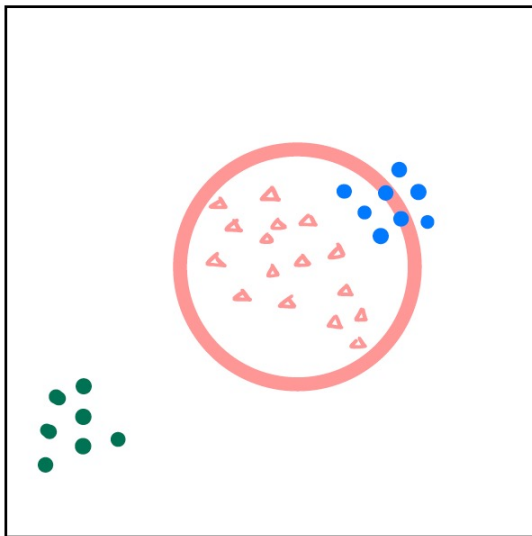
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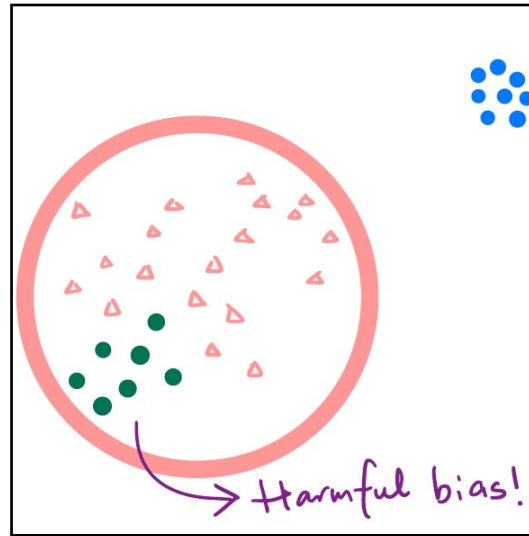
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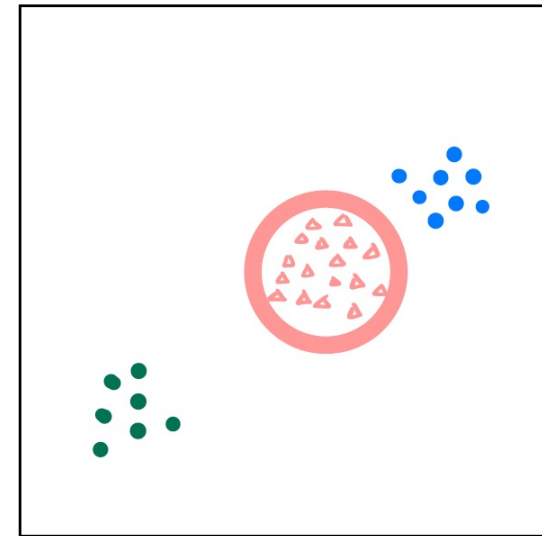
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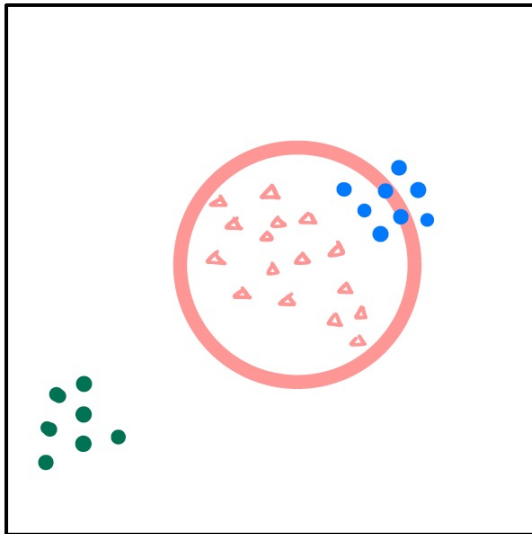
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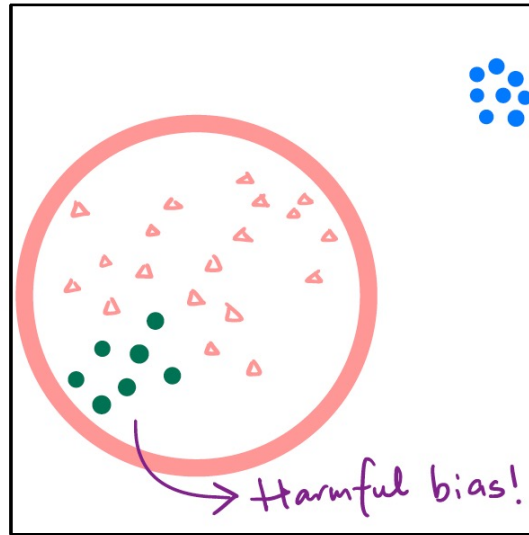
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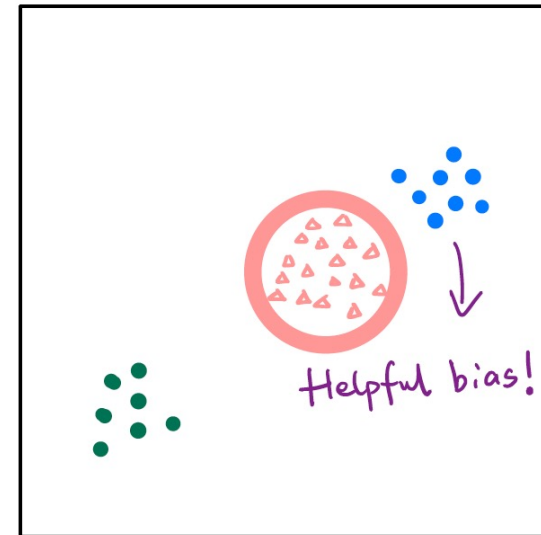
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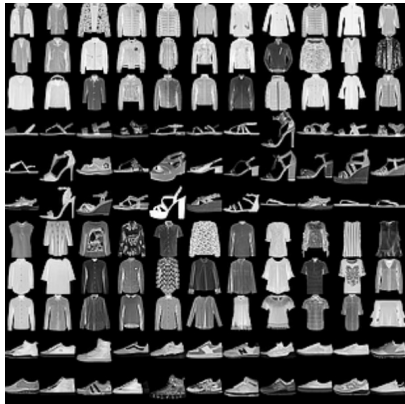


# Experiment Setup

## Models

Type	Semi-supervised (trained on normal data)	Supervised (trained on normal & some abnormal data)
Hypersphere-based	Deep SVDD [Ruff <i>et al.</i> , 2018]	Deep SAD [Ruff <i>et al.</i> , 2020b], Hypersphere Classifier (HSC) [Ruff <i>et al.</i> , 2020a]
Reconstruction-based	Autoencoder (AE) [Zhou and Paffenroth, 2017]	Supervised AE (SAE) <sup>7</sup> , Autoencoding Binary Classifier (ABC) [Yamanaka <i>et al.</i> , 2019]

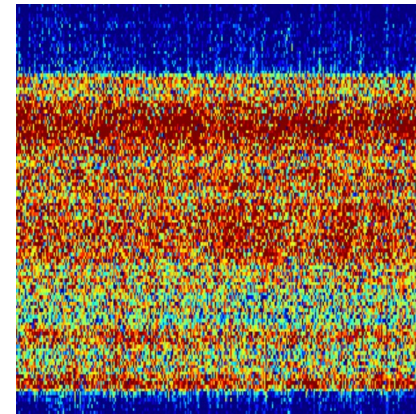
## Datasets



Fashion-MNIST

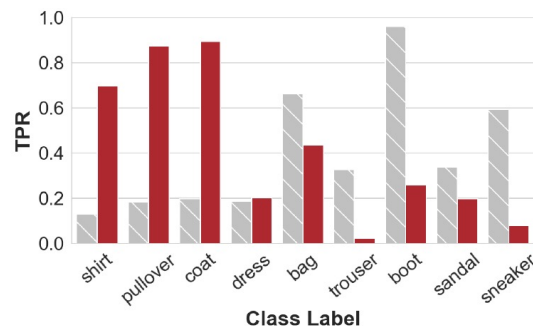


Landsat Satellite



Spectrum Misuse

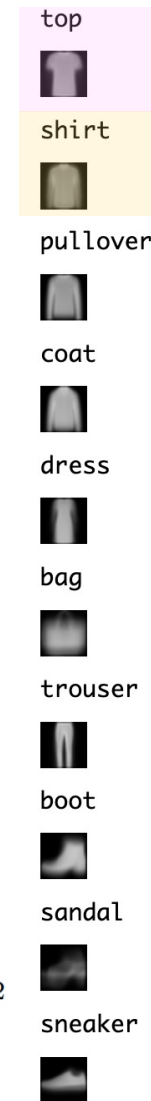
# Scenario 1: Training w/ the *Hard* Anomalies



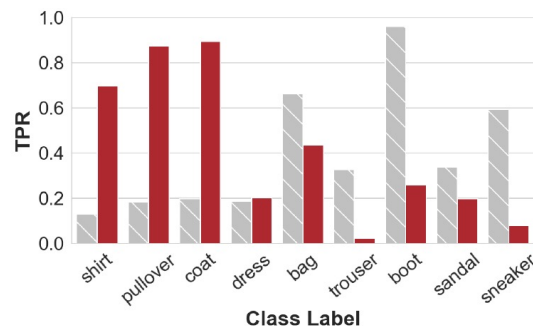
training normal = top, training abnormal = shirt

Test data	Deep SVDD	Deep SAD	HSC	AE	SAE	ABC	$L^2$ to shirt
shirt	0.09 ± 0.01	0.71 ± 0.01 ↑	0.70 ± 0.01 ↑	0.12 ± 0.01	0.72 ± 0.01 ↑	0.72 ± 0.01 ↑	0
pullover	0.13 ± 0.02	0.90 ± 0.01 ↑	0.89 ± 0.01 ↑	0.19 ± 0.02	0.84 ± 0.02 ↑	0.85 ± 0.01 ↑	0.01
coat	0.14 ± 0.03	0.92 ± 0.02 ↑	0.92 ± 0.01 ↑	0.15 ± 0.02	0.92 ± 0.02 ↑	0.92 ± 0.01 ↑	0.01
dress	0.17 ± 0.03	0.24 ± 0.03 ↑	0.24 ± 0.03 ↑	0.11 ± 0.01	0.20 ± 0.03 ↑	0.21 ± 0.03 ↑	0.04
bag	0.49 ± 0.07	0.38 ± 0.08 ↓	0.36 ± 0.07 ↓	0.70 ± 0.03	0.52 ± 0.09 ↓	0.53 ± 0.07 ↓	0.04
trouser	0.32 ± 0.10	0.07 ± 0.04 ↓	0.06 ± 0.03 ↓	0.59 ± 0.04	0.07 ± 0.04 ↓	0.16 ± 0.07 ↓	0.06
boot	0.92 ± 0.03	0.29 ± 0.15 ↓	0.27 ± 0.16 ↓	0.98 ± 0.02	0.90 ± 0.09 ↓	0.90 ± 0.08 ↓	0.08
sandal	0.30 ± 0.04	0.26 ± 0.08 ↓	0.26 ± 0.12 ↓	0.82 ± 0.02	0.46 ± 0.10 ↓	0.56 ± 0.09 ↓	0.09
sneaker	0.55 ± 0.09	0.12 ± 0.10 ↓	0.14 ± 0.12 ↓	0.74 ± 0.09	0.47 ± 0.19 ↓	0.46 ± 0.18 ↓	0.10

Table 3: The model TPR under scenario 1, Fashion-MNIST. The normal class top is similar to the abnormal training class shirt. Their  $L^2$  distance = 0.02.



# Scenario 1: Training w/ the *Hard* Anomalies



Positive bias!

training normal = top, training abnormal = shirt

Test data	Deep SVDD	Deep SAD	HSC	AE	SAE	ABC	$L^2$ to shirt
shirt	0.09 ± 0.01	0.71 ± 0.01 ↑	0.70 ± 0.01 ↑	0.12 ± 0.01	0.72 ± 0.01 ↑	0.72 ± 0.01 ↑	0
pullover	0.13 ± 0.02	0.90 ± 0.01 ↑	0.89 ± 0.01 ↑	0.19 ± 0.02	0.84 ± 0.02 ↑	0.85 ± 0.01 ↑	0.01
coat	0.14 ± 0.03	0.92 ± 0.02 ↑	0.92 ± 0.01 ↑	0.15 ± 0.02	0.92 ± 0.02 ↑	0.92 ± 0.01 ↑	0.01
dress	0.17 ± 0.03	0.24 ± 0.03 ↑	0.24 ± 0.03 ↑	0.11 ± 0.01	0.20 ± 0.03 ↑	0.21 ± 0.03 ↑	0.04
bag	0.49 ± 0.07	0.38 ± 0.08 ↓	0.36 ± 0.07 ↓	0.70 ± 0.03	0.52 ± 0.09 ↓	0.53 ± 0.07 ↓	0.04
trouser	0.32 ± 0.10	0.07 ± 0.04 ↓	0.06 ± 0.03 ↓	0.59 ± 0.04	0.07 ± 0.04 ↓	0.16 ± 0.07 ↓	0.06
boot	0.92 ± 0.03	0.29 ± 0.15 ↓	0.27 ± 0.16 ↓	0.98 ± 0.02	0.90 ± 0.09 ↓	0.90 ± 0.08 ↓	0.08
sandal	0.30 ± 0.04	0.26 ± 0.08 ↓	0.26 ± 0.12 ↓	0.82 ± 0.02	0.46 ± 0.10 ↓	0.56 ± 0.09 ↓	0.09
sneaker	0.55 ± 0.09	0.12 ± 0.10 ↓	0.14 ± 0.12 ↓	0.74 ± 0.09	0.47 ± 0.19 ↓	0.46 ± 0.18 ↓	0.10

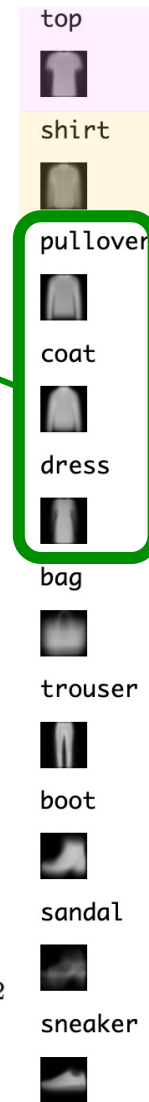
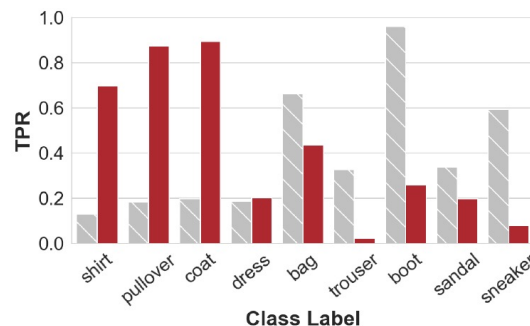


Table 3: The model TPR under scenario 1, Fashion-MNIST. The normal class top is similar to the abnormal training class shirt. Their  $L^2$  distance = 0.02.

# Scenario 1: Training w/ the *Hard* Anomalies



training normal = top, training abnormal = shirt

Test data	Deep SVDD	Deep SAD	HSC	AE	SAE	ABC	$L^2$ to shirt
shirt	0.09 ± 0.01	0.71 ± 0.01 ↑	0.70 ± 0.01 ↑	0.12 ± 0.01	0.72 ± 0.01 ↑	0.72 ± 0.01 ↑	0
pullover	0.13 ± 0.02	0.90 ± 0.01 ↑	0.89 ± 0.01 ↑	0.19 ± 0.02	0.84 ± 0.02 ↑	0.85 ± 0.01 ↑	0.01
coat	0.14 ± 0.03	0.92 ± 0.02 ↑	0.92 ± 0.01 ↑	0.15 ± 0.02	0.92 ± 0.02 ↑	0.92 ± 0.01 ↑	0.01
dress	0.17 ± 0.03	0.24 ± 0.03 ↑	0.24 ± 0.03 ↑	0.11 ± 0.01	0.20 ± 0.03 ↑	0.21 ± 0.03 ↑	0.04
bag	0.49 ± 0.07	0.38 ± 0.08 ↓	0.36 ± 0.07 ↓	0.70 ± 0.03	0.52 ± 0.09 ↓	0.53 ± 0.07 ↓	0.04
trouser	0.32 ± 0.10	0.07 ± 0.04 ↓	0.06 ± 0.03 ↓	0.59 ± 0.04	0.07 ± 0.04 ↓	0.16 ± 0.07 ↓	0.06
boot	0.92 ± 0.03	0.29 ± 0.15 ↓	0.27 ± 0.16 ↓	0.98 ± 0.02	0.90 ± 0.09 ↓	0.90 ± 0.08 ↓	0.08
sandal	0.30 ± 0.04	0.26 ± 0.08 ↓	0.26 ± 0.12 ↓	0.82 ± 0.02	0.46 ± 0.10 ↓	0.56 ± 0.09 ↓	0.09
sneaker	0.55 ± 0.09	0.12 ± 0.10 ↓	0.14 ± 0.12 ↓	0.74 ± 0.09	0.47 ± 0.19 ↓	0.46 ± 0.18 ↓	0.10

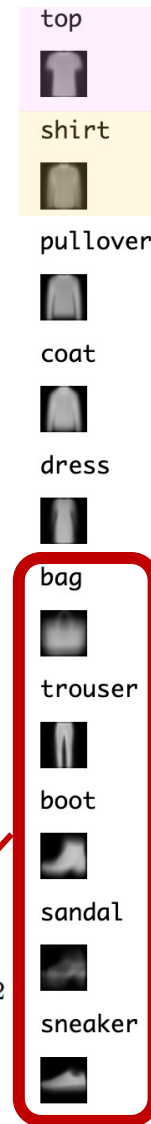
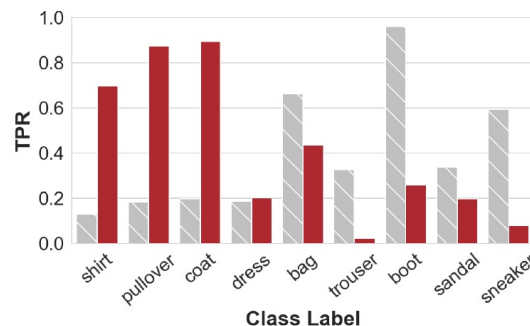


Table 3: The model TPR under scenario 1, Fashion-MNIST. The normal class top is similar to the abnormal training class shirt. Their  $L^2$  distance = 0.02.

*Negative bias!*

# Scenario 1: Training w/ the *Hard* Anomalies



*Positive bias!*

training normal = top, training abnormal = shirt

Test data	Deep SVDD	Deep SAD	HSC	AE	SAE	ABC	$L^2$ to shirt
shirt	0.09 ± 0.01	0.71 ± 0.01 ↑	0.70 ± 0.01 ↑	0.12 ± 0.01	0.72 ± 0.01 ↑	0.72 ± 0.01 ↑	0
pullover	0.13 ± 0.02	0.90 ± 0.01 ↑	0.89 ± 0.01 ↑	0.19 ± 0.02	0.84 ± 0.02 ↑	0.85 ± 0.01 ↑	0.01
coat	0.14 ± 0.03	0.92 ± 0.02 ↑	0.92 ± 0.01 ↑	0.15 ± 0.02	0.92 ± 0.02 ↑	0.92 ± 0.01 ↑	0.01
dress	0.17 ± 0.03	0.24 ± 0.03 ↑	0.24 ± 0.03 ↑	0.11 ± 0.01	0.20 ± 0.03 ↑	0.21 ± 0.03 ↑	0.04
bag	0.49 ± 0.07	0.38 ± 0.08 ↓	0.36 ± 0.07 ↓	0.70 ± 0.03	0.52 ± 0.09 ↓	0.53 ± 0.07 ↓	0.04
trouser	0.32 ± 0.10	0.07 ± 0.04 ↓	0.06 ± 0.03 ↓	0.59 ± 0.04	0.07 ± 0.04 ↓	0.16 ± 0.07 ↓	0.06
boot	0.92 ± 0.03	0.29 ± 0.15 ↓	0.27 ± 0.16 ↓	0.98 ± 0.02	0.90 ± 0.09 ↓	0.90 ± 0.08 ↓	0.08
sandal	0.30 ± 0.04	0.26 ± 0.08 ↓	0.26 ± 0.12 ↓	0.82 ± 0.02	0.46 ± 0.10 ↓	0.56 ± 0.09 ↓	0.09
sneaker	0.55 ± 0.09	0.12 ± 0.10 ↓	0.14 ± 0.12 ↓	0.74 ± 0.09	0.47 ± 0.19 ↓	0.46 ± 0.18 ↓	0.10

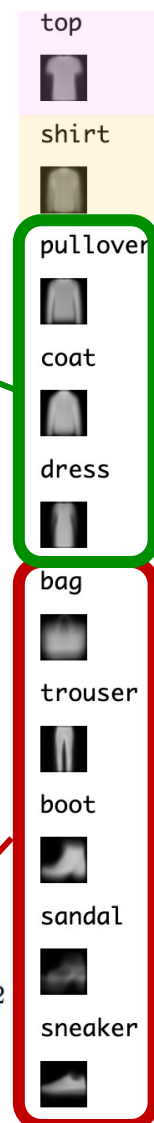
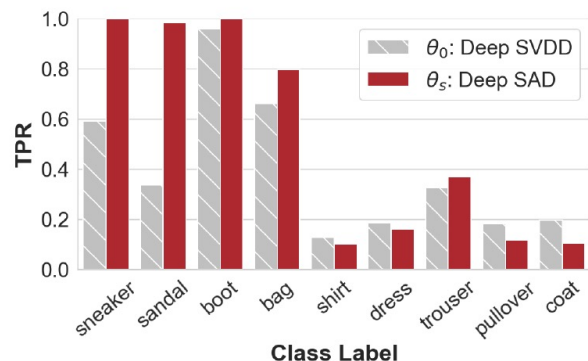


Table 3: The model TPR under scenario 1, Fashion-MNIST. The normal class top is similar to the abnormal training class shirt. Their  $L^2$  distance = 0.02.

*Negative bias!*



## Scenario 2: Training w/ the *Easy* Anomalies



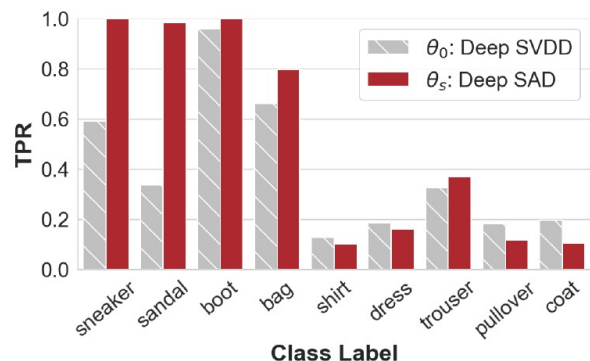
training normal = top, training abnormal = sneaker

Test data	Deep SVDD	Deep SAD	HSC	AE	SAE	ABC	$L^2$ to sneaker
sneaker	$0.55 \pm 0.09$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	$0.74 \pm 0.09$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	0
sandal	$0.30 \pm 0.04$	$0.99 \pm 0.01 \uparrow$	$0.98 \pm 0.02 \uparrow$	$0.82 \pm 0.02$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	0.02
boot	$0.92 \pm 0.03$	$1.00 \pm 0.00 \uparrow$	$0.97 \pm 0.02 \uparrow$	$0.98 \pm 0.02$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	0.07
bag	$0.49 \pm 0.07$	$0.80 \pm 0.05 \uparrow$	$0.81 \pm 0.11 \uparrow$	$0.70 \pm 0.03$	$0.84 \pm 0.03 \uparrow$	$0.82 \pm 0.03 \uparrow$	0.07
shirt	$0.09 \pm 0.01$	$0.11 \pm 0.02 \uparrow$	$0.12 \pm 0.01 \uparrow$	$0.12 \pm 0.01$	$0.13 \pm 0.01 \uparrow$	$0.15 \pm 0.01 \uparrow$	0.10
trouser	$0.32 \pm 0.09$	$0.31 \pm 0.10$	$0.11 \pm 0.12 \downarrow$	$0.58 \pm 0.04$	$0.58 \pm 0.03$	$0.58 \pm 0.05$	0.12
dress	$0.16 \pm 0.03$	$0.16 \pm 0.04$	$0.11 \pm 0.01 \downarrow$	$0.11 \pm 0.01$	$0.11 \pm 0.01$	$0.12 \pm 0.01$	0.13
pullover	$0.13 \pm 0.02$	$0.13 \pm 0.03$	$0.14 \pm 0.05$	$0.19 \pm 0.02$	$0.21 \pm 0.03$	$0.19 \pm 0.02$	0.13
coat	$0.14 \pm 0.03$	$0.13 \pm 0.03$	$0.13 \pm 0.06$	$0.15 \pm 0.02$	$0.16 \pm 0.02$	$0.15 \pm 0.02$	0.14

Table 6: The model TPR under scenario 2, Fashion-MNIST. The normal class top is dissimilar to the abnormal training class sneaker, and the  $L^2$  distance between the two is 0.13.



## Scenario 2: Training w/ the *Easy* Anomalies

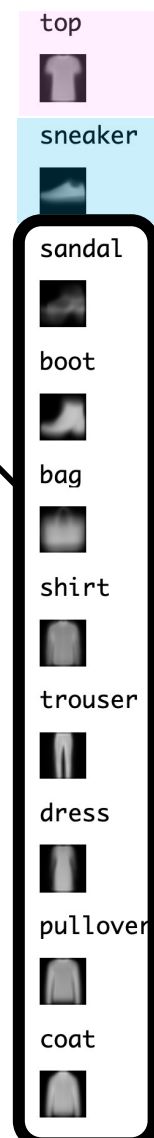


*Mostly harmless bias!*

training normal = top, training abnormal = sneaker

Test data	Deep SVDD	Deep SAD	HSC	AE	SAE	ABC	$L^2$ to sneaker
sneaker	0.55 ± 0.09	1.00 ± 0.00 ↑	1.00 ± 0.00 ↑	0.74 ± 0.09	1.00 ± 0.00 ↑	1.00 ± 0.00 ↑	0
sandal	0.30 ± 0.04	0.99 ± 0.01 ↑	0.98 ± 0.02 ↑	0.82 ± 0.02	1.00 ± 0.00 ↑	1.00 ± 0.00 ↑	0.02
boot	0.92 ± 0.03	1.00 ± 0.00 ↑	0.97 ± 0.02 ↑	0.98 ± 0.02	1.00 ± 0.00 ↑	1.00 ± 0.00 ↑	0.07
bag	0.49 ± 0.07	0.80 ± 0.05 ↑	0.81 ± 0.11 ↑	0.70 ± 0.03	0.84 ± 0.03 ↑	0.82 ± 0.03 ↑	0.07
shirt	0.09 ± 0.01	0.11 ± 0.02 ↑	0.12 ± 0.01 ↑	0.12 ± 0.01	0.13 ± 0.01 ↑	0.15 ± 0.01 ↑	0.10
trouser	0.32 ± 0.09	0.31 ± 0.10	0.11 ± 0.12 ↓	0.58 ± 0.04	0.58 ± 0.03	0.58 ± 0.05	0.12
dress	0.16 ± 0.03	0.16 ± 0.04	0.11 ± 0.01 ↓	0.11 ± 0.01	0.11 ± 0.01	0.12 ± 0.01	0.13
pullover	0.13 ± 0.02	0.13 ± 0.03	0.14 ± 0.05	0.19 ± 0.02	0.21 ± 0.03	0.19 ± 0.02	0.13
coat	0.14 ± 0.03	0.13 ± 0.03	0.13 ± 0.06	0.15 ± 0.02	0.16 ± 0.02	0.15 ± 0.02	0.14

Table 6: The model TPR under scenario 2, Fashion-MNIST. The normal class top is dissimilar to the abnormal training class sneaker, and the  $L^2$  distance between the two is 0.13.



## Scenario 3: Mixed Training

training normal = top, training abnormal = 50% shirt and 50% sneaker

Test data	Deep SVDD	Deep SAD	HSC	AE	SAE	ABC	$L^2$ to shirt	$L^2$ to sneaker
shirt	$0.09 \pm 0.01$	$0.69 \pm 0.01 \uparrow$	$0.69 \pm 0.02 \uparrow$	$0.12 \pm 0.01$	$0.67 \pm 0.01 \uparrow$	$0.66 \pm 0.01 \uparrow$	0	0.10
sneaker	$0.55 \pm 0.09$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	$0.74 \pm 0.09$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	0.10	0
pullover	$0.13 \pm 0.02$	$0.90 \pm 0.01 \uparrow$	$0.90 \pm 0.01 \uparrow$	$0.19 \pm 0.02$	$0.82 \pm 0.02 \uparrow$	$0.83 \pm 0.02 \uparrow$	0.01	0.13
coat	$0.14 \pm 0.03$	$0.91 \pm 0.02 \uparrow$	$0.90 \pm 0.01 \uparrow$	$0.15 \pm 0.02$	$0.86 \pm 0.02 \uparrow$	$0.87 \pm 0.02 \uparrow$	0.01	0.14
dress	$0.17 \pm 0.03$	$0.23 \pm 0.04 \uparrow$	$0.24 \pm 0.04 \uparrow$	$0.11 \pm 0.01$	$0.19 \pm 0.03 \uparrow$	$0.18 \pm 0.02 \uparrow$	0.04	0.13
bag	$0.49 \pm 0.07$	$0.63 \pm 0.06 \uparrow$	$0.62 \pm 0.07 \uparrow$	$0.70 \pm 0.03$	$0.76 \pm 0.05 \uparrow$	$0.78 \pm 0.03 \uparrow$	0.04	0.07
trouser	$0.32 \pm 0.10$	$0.05 \pm 0.04 \downarrow$	$0.04 \pm 0.02 \downarrow$	$0.59 \pm 0.04$	$0.22 \pm 0.08 \downarrow$	$0.34 \pm 0.06 \downarrow$	0.06	0.12
boot	$0.92 \pm 0.03$	$0.95 \pm 0.03$	$0.95 \pm 0.03$	$0.98 \pm 0.02$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	0.08	0.07
sandal	$0.30 \pm 0.04$	$0.92 \pm 0.04 \uparrow$	$0.92 \pm 0.04 \uparrow$	$0.82 \pm 0.02$	$0.96 \pm 0.01 \uparrow$	$0.97 \pm 0.01 \uparrow$	0.09	0.02

Table 9: The model TPR under configuration 1 of weighted mixture training on Fashion-MNIST.

# Takeaways and Future Directions

- Additional labeled data in AD poses a hidden threat for model practitioners.
- **Potential debiasing strategies:**
  - **Data-based strategy**
    - Using active learning and to get representative anomaly labels on the fly.
    - Leveraging synthetic samples;
  - **Model-based strategy**
    - *Robust* model design (e.g., ensembles).

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